

New measurement of the $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ branching ratio

version 1

E949 collaboration

July 25, 2008

Abstract

Three candidates for the decay $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ have been observed in the pion momentum region $140 < P < 199$ MeV/ c upon an estimated background of $0.927 \pm 0.168^{+0.320}_{-0.237}$ events. Combining these observations with previously reported results yields a branching fraction of $\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (1.73^{+1.15}_{-1.05}) \times 10^{-10}$.

The rate of $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ decays is amongst a handful of hadronic processes that can be accurately predicted in the standard model (SM) owing to knowledge of the transition matrix element from similar processes and minimal long-distance effects [1]. The small precisely predicted branching fraction, $\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (0.85 \pm 0.07) \times 10^{-10}$ [2], and the fact that this decay is a flavor changing neutral current process makes it a sensitive probe of non-SM effects [1]. Previous studies of this decay by experiment E787 at Brookhaven National Laboratory and its successor E949 have measured $\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (1.47^{+1.30}_{-0.89}) \times 10^{-10}$ based on the observation of three candidates upon a total background of 0.44 ± 0.05 events in the pion momentum

22 region $211 < P < 229$ MeV/ c (pnn1) above the $K^+ \rightarrow \pi^+\pi^0$ ($K_{\pi 2}$) peak [3]
 23 and set a consistent limit of $< 22 \times 10^{-10}$ at 90% C.L. based on one candi-
 24 date upon a total background of 1.22 ± 0.24 events in the momentum region
 25 $140 < P < 195$ MeV/ c (pnn2) below the $K_{\pi 2}$ peak [6].

26 In this Letter we report the results of a search for $K^+ \rightarrow \pi^+\nu\bar{\nu}$ below the
 27 $K_{\pi 2}$ peak using 1.7×10^{12} stopped K^+ decays obtained with E949 as well as
 28 the final results on $\mathcal{B}(K^+ \rightarrow \pi^+\nu\bar{\nu})$ from all E787 and E949 data.

29 The E949 apparatus and analysis of the data in the pnn1 region has been
 30 described elsewhere [4]. In this Letter, we concentrate on the apparatus and
 31 analysis features most relevant for pnn2. Identification of $K^+ \rightarrow \pi^+\nu\bar{\nu}$ de-
 32 cays relies on detection of an incoming kaon and outgoing pion with no other
 33 detector activity. A 710 MeV/ c K^+ beam, produced by 21.5 GeV proton
 34 interactions on a platinum target, passed through two electromagnetostatic
 35 separators during transport to the E949 scintillating fiber target (TG). Typ-
 36 ically 1.6×10^6 K^+ /s entered the E949 TG during a 2.2 s spill with a K^+/π^+
 37 ratio of ~ 3 .

38 Incoming kaons were identified by a Cerenkov counter and two propor-
 39 tional wire chambers before being slowed by an 11.1 cm thick BeO degrader
 40 and an active degrader (AD), passing through a beam hodoscope and stop-
 41 ping in the TG. The AD comprised 39 2.2 mm thick copper disks interleaved
 42 with 40 layers of 2.2 mm plastic scintillator divided into 12 azimuthal seg-
 43 ments. Scintillation light from each segment was transported via wavelength
 44 shifting fibers to a photomultiplier tube (PMT) that was read out by time-

45 to-digital convertors (TDCs), GaAs CCD digitizers (CCDs) sampling at 500
 46 MHz and analog-to-digital convertors (ADCs). The AD was capable of pro-
 47 viding measurements of the incoming beam particle and activity coincident
 48 with K^+ decay in the TG. The TG consists of 413 5mm square and 3.1 m
 49 long scintillating fibers packed into a 12 cm diameter cylinder. Each 5 mm
 50 fiber was connected to a PMT and read out by ADCs, TDCs and CCDs in
 51 order to provide measurements of activity in the TG coincident with both
 52 the incoming kaon and the outgoing pion.

53 The momentum, trajectory and position of the outgoing π^+ were mea-
 54 sured in a drift chamber [7]. The outgoing pion was slowed to a stop in
 55 a range stack (RS) of 19 layers of plastic scintillator with 24 segments in
 56 azimuth. PMTs on each end of the scintillator were read out by ADCs,
 57 TDCs and 500-MHz transient digitizers (TDs) and enabled measurement of
 58 the pion range (R) and kinetic energy (E) as well as the $\pi^+ \rightarrow \mu^+ \rightarrow e^+$
 59 decay sequence.

60 The barrel veto (BV) calorimeters of 16.6 radiation lengths at normal in-
 61 cidence provided photon vetoing over $2/3$ of 4π sr solid angle. Photon vetoing
 62 over the remaining $1/3$ of 4π was provided by upstream and downstream end
 63 caps of undoped CsI (13.5 r.l.), upstream (4.6 r.l.) and downstream (9.2 r.l.)
 64 collar counters, a downstream microcollar (~ 15 r.l.), an upstream photon
 65 veto (3.1 r.l.) and a downstream photon veto (DPV, 7.3 r.l.). The latter de-
 66 tectors all utilized lead/scintillator technology. The AD (6.1 r.l.) and target
 67 (~ 7.3 r.l.) also provided additional photon veto capability [4].

68 Data were acquired with a multilevel trigger that required an entering
 69 kaon to stop in the target followed by an outgoing particle leaving the tar-
 70 get at least 1.5 ns later that was subsequently identified as a pion via the
 71 $\pi^+ \rightarrow \mu^+$ signature in the RS TD read out and accompanied by no other ac-
 72 tivity. Additional pre-scaled triggers were used to accumulate $K^+ \rightarrow \mu^+ \nu(\gamma)$
 73 ($K_{\mu 2(\gamma)}$) and $K_{\pi 2}$ decays as well as beam pions scattering in the target for
 74 monitoring and calibration purposes.

75 This analysis exploited previous experience [4] [5] [6] as well as detector
 76 upgrades of the AD, BV and DPV to increase signal acceptance by 40%
 77 compared to [6] while maintaining a comparable background rate. In addition
 78 the improved knowledge of the background contributions allowed the signal
 79 region to be divided into 9 sub-regions (“cells”) with relative acceptance-to-
 80 background levels differing by a factor of ~ 4 that could be exploited by a
 81 likelihood method [8] to determine $\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$.

82 We employed a “blind” analysis technique in which the signal region was
 83 not examined until all signal candidate selection criteria (“cuts”) were es-
 84 tablished, the estimate of all backgrounds were completed and acceptance of
 85 all cells determined. At least two uncorrelated cuts with significant rejec-
 86 tion were created for most backgrounds. Inversion of one of the pair of cuts
 87 could then be used to select a background-enriched data sample containing N
 88 events. Inversion of the complementary cut selected a data sample on which
 89 the rejection \mathcal{R} of the first cut could be measured. The background was esti-
 90 mated as $N/(\mathcal{R} - 1)$. We ensured unbiased background estimates by dividing

91 the data into one-third and two-third samples selected uniformly from the
 92 entire data set. Selection criteria were determined with the one-third sam-
 93 ple and background estimated from the two-third sample. In contrast to
 94 the analysis of the pnn1 region, some backgrounds do not have sufficiently
 95 distinct characteristics to permit isolation by cut inversion of a pure back-
 96 ground sample and permit a measurement of \mathcal{R} with the data. For these
 97 backgrounds, we resorted to simulated data to estimate \mathcal{R} .

98 The largest background was due to $K_{\pi 2}$ decays in which the π^+ inelasti-
 99 cally scatters in the TG, losing energy and obscuring the directional correla-
 100 tion with the photons from the π^0 decay that would otherwise be detected in
 101 the barrel. The two cuts that suppressed this background were identification
 102 of π^+ scattering and detection of the photons from π^0 decay. The latter pho-
 103 ton veto (PV) ability was improved in E949 with respect to E787 primarily
 104 due to the AD and augmentation of the BV by 2.3 r.l. Pion scattering was
 105 identified by kinks in the pattern of TG fibers attributed to the outgoing
 106 pion, tracks that did not point back to the fiber containing the K^+ decay,
 107 energy deposits inconsistent with an outgoing pion or energy deposited in
 108 fibers traversed by the kaon at the time of the outgoing pion. The “CCD-
 109 PUL” cut identified the latter signature by performing a least-squares fit to
 110 the CCD samples to identify the pulses due to activity coincident with the
 111 kaon and pion. The uncertainty in the $K_{\pi 2}$ TG-scatter background has com-
 112 parable statistical and systematic contributions (Table 1). The systematic
 113 uncertainty was determined by the range of PV rejection values measured

on samples of $K_{\pi 2}$ scatter events selected by different scattering signatures in the TG or in different kinematic regions. There was also a much smaller background from $K_{\pi 2}$ due to scattering in the RS that was identified by the pattern of RS counters and the energy deposited by the track.

Additional backgrounds included $K^+ \rightarrow \pi^+ \pi^0 \gamma$ ($K_{\pi 2 \gamma}$), $K^+ \rightarrow \pi^+ \pi^- e^+ \nu$ (K_{e4}), $K^+ \mu^+ \nu(\gamma)$ and $K^+ \rightarrow \pi^0 \mu^+ \nu$ (muon), scattered beam pions (beam) and $K_L^0 \rightarrow \pi^+ \ell^- \bar{\nu}$ where $\ell^+ = e^+$ or μ^+ resulting from K^+ charge-exchange (CEX) reactions. Simulated data were used to estimate the rejection \mathcal{R} of the cuts that suppress K_{e4} , $K_{\pi 2 \gamma}$ and CEX backgrounds. These backgrounds could not be distinguished from the larger $K_{\pi 2}$ -scatter background based solely on the π^+ track. The K_{e4} process forms a background when the π^- and e^+ interact in the TG without leaving a detectable trace. Positron interactions are well-modelled in our EGS-based simulation [9] and we used the π^- energy deposition spectrum in scintillator measured previously in E787 [10] to model π^- absorption. We assessed the systematic uncertainty in the K_{e4} background by varying the threshold of cuts on the energy deposited both in the kaon fibers at pion time and in non-kaon and non-pion fibers. The kinematics cuts (KIN) defining the entire signal region were $140 < P < 199$ MeV/ c , $60 < E < 100.5$ MeV and $12 < R < 28$ cm. We defined a smaller region $165 < P < 197$ MeV/ c , $72 < E < 100$ MeV and $17 < R < 28$ cm where the lower and upper limits were chosen to suppress the K_{e4} background that peaks near 160 MeV/ c and the tail of the $K_{\pi 2}$ peak, respectively.

Measurement of the K^+ charge-exchange reaction was used as input to

137 simulate CEX events [4]. The requirement on the delayed coincidence (DC)
 138 between the reconstructed kaon and pion candidates provides suppression of
 139 CEX background as the emitted π^+ was required to be within the fiducial
 140 region of the TG. The systematic uncertainty was assessed with the same
 141 methodology as the K_{e4} background.

142 The rejection of the $K_{\pi 2\gamma}$ background of the kinematic cuts was calculated
 143 using a combination of simulated $K_{\pi 2}$ and $K_{\pi 2\gamma}$ events and $K_{\pi 2}$ data events.
 144 The additional PV rejection due to the radiative photon was calculated from
 145 the photon distribution in simulated events and the rejection power of single
 146 photons as a function of angle and energy evaluated with $K_{\pi 2}$ data [11].

147 The remaining muon and beam backgrounds were estimated entirely from
 148 data and were very small (Table 1). As previous analyses had shown the
 149 muon background to be small [5] [6], the TD-based requirements on $\pi^+ \rightarrow$
 150 $\mu^+ \rightarrow e^+$ identification were loosened to gain acceptance.

151 The signal region was divided into 9 cells using standard (*s*) and more
 152 restrictive (*r*) versions of the KIN, TD, DC and PV cuts. The signal region
 153 was first divided into two regions defined by $\text{KIN}_s \cdot \overline{\text{KIN}}_r \cdot \text{TD}_s \cdot \text{DC}_s \cdot \text{PV}_s$ and
 154 $\text{KIN}_r \cdot \text{TD}_s \cdot \text{DC}_s \cdot \text{PV}_s$. The former region was defined as 1 cell and the latter
 155 region was further subdivided into 8 additional cells using the permutations
 156 of the TD, DC and PV cuts. The background and acceptance of the best
 157 cell, defined as $\text{KIN}_r \cdot \text{TD}_r \cdot \text{DC}_r \cdot \text{PV}_r$, is given in Table 1.

158 The reliability of the background estimates was checked by loosening the
 159 PV and CCDPUL cuts to define three regions just outside the signal region.

160 Two of the regions, PV_1 and $CCDPUL_1$, were immediately adjacent to the
 161 signal region whilst a third region PV_2 was defined by further loosening of the
 162 PV cut. The number of expected and observed events and the probability of
 163 the observation are given in Table 2. The 5.1% probability for the regions
 164 nearest the signal region may have indicated that the background was over-
 165 estimated. Given the inability to cleanly isolate each background component
 166 by cut inversion, some contamination is possible and would generally inflate
 167 the background estimates. Re-evaluation of the probabilities at the lower
 168 limit of the systematic uncertainties gave 13.0% for the two closest regions
 169 and demonstrated that the assigned systematic uncertainties were reasonable.

170 After completion of the background studies, the signal region was ex-
 171 amined and three candidates were found. The energy vs range for the ob-
 172 served candidates is shown in Figure 1 along with the results of previous
 173 E787 [3] and E949 [6] analyses. From the observed events, $\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) =$
 174 $(7.89^{+9.26}_{-5.10}) \times 10^{-10}$ was calculated using the likelihood method [8] taking into
 175 account the uncertainties in the background and acceptance measurements.
 176 When combined with the results of previous E787 [3] and E949 [6] analyses,
 177 $\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (1.73^{+1.15}_{-1.05}) \times 10^{-10}$ or $< 3.35 \times 10^{-10}$ at 90% CL. This
 178 result is consistent with the SM prediction. Assuming $\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) =$
 179 1.73×10^{-10} , the signal-to-background (S/B) ratios for the three candidates
 180 are 0.20, 0.42 and 0.48, which can be compared with the S/B = 0.20 for the
 181 previous pnn2 candidate [5] and S/B = 59, 8.2 and 1.1 for the pnn1 candi-
 182 dates [3]. As an indication of the improvements in the analysis, a candidate

Bkgd comp.	Cut and additional rejection or acceptance loss					Entire region	Best cell
	KIN	TD	DC	PV	REC		
$K_{\pi 2}$ TG	1.63			2.75	✓	$0.619 \pm 0.150^{+0.067}_{-0.100}$	$0.102 \pm 0.024^{+0.011}_{-0.017}$
$K_{\pi 2}$ RS	1.63			2.75	✓	$0.030 \pm 0.005 \pm 0.004$	$0.005 \pm 0.001 \pm 0.001$
$K_{\pi 2\gamma}$	1.20			✓		$0.076 \pm 0.007 \pm 0.006$	$0.017 \pm 0.002 \pm 0.001$
K_{e4}	2.70			✓		$0.176 \pm 0.072^{+0.233}_{-0.124}$	$0.025 \pm 0.010^{+0.033}_{-0.018}$
CEX			6.7	✓		$0.013 \pm 0.013^{+0.010}_{-0.003}$	$0.001 \pm 0.001^{+0.001}_{-0.000}$
Muon		3.08			✓	0.011 ± 0.011	0.001 ± 0.001
Beam			1.0	✓		0.001 ± 0.001	< 0.001
Total background						$0.927 \pm 0.168^{+0.320}_{-0.237}$	$0.152 \pm 0.027^{+0.047}_{-0.036}$
Acc.	0.812	0.812	0.911	0.522	NA		

Table 1: Summary of the applicable cuts, additional rejection or acceptance loss, contributions to the entire signal region and best cell for each background component. The middle columns indicate the additional rejection for each component from the tightening of the kinematic (KIN), TD, delayed coincidence (DC), photon veto (PV) and reconstruction (REC) cuts. A ✓ indicates that the cut was inverted to determine the background. The bottom row gives the relative acceptance loss associated with tightening each cut to divide the signal region into 9 cells. The acceptance of the entire region and best cell was $(1.366 \pm 0.016 \pm 0.052) \times 10^{-3}$ and $(0.436 \pm 0.007^{+0.015}_{-0.019}) \times 10^{-3}$, respectively.

183 in the best cell (Table 1) would have had S/B=0.84. The probability that the
184 three observed candidates are due to background only, given the estimated
185 background in each cell, is 0.037. The probability that all $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ can-
186 didates [3] [6] are due to background is 0.001.

187 Thanks to the usual agencies for their support and the fantastic operation
188 of the AGS.

Region	N_{exp}	N_{obs}	$\mathcal{P}(\leq N_{\text{obs}}; N_{\text{exp}})$	Combined
CCD_1	$0.79 \pm 0.35^{+0.30}_{-0.37}$	0	0.452 (0.652)	NA
PV_1	$9.09 \pm 0.65^{+1.38}_{-1.15}$	3	0.020 (0.044)	0.051 (0.130)
PV_2	$32.4 \pm 1.9^{+12.2}_{-7.9}$	34	0.613 (0.973)	0.140 (0.390)

Table 2: Comparison of the expected N_{exp} and observed N_{obs} number of events in three regions CCD_1 , PV_1 and PV_2 near the signal region. The central value of N_{exp} is given along with the statistical and systematic uncertainties. $\mathcal{P}(\leq N_{\text{obs}}; N_{\text{exp}})$ is the probability of observing N_{obs} events or fewer when N_{exp} events are expected. The rightmost column “Combined” gives the probability of the combined observation in that region and the region(s) of the preceding row(s). The numbers in parentheses are the probabilities re-evaluated when N_{exp} is reduced by the systematic uncertainty.

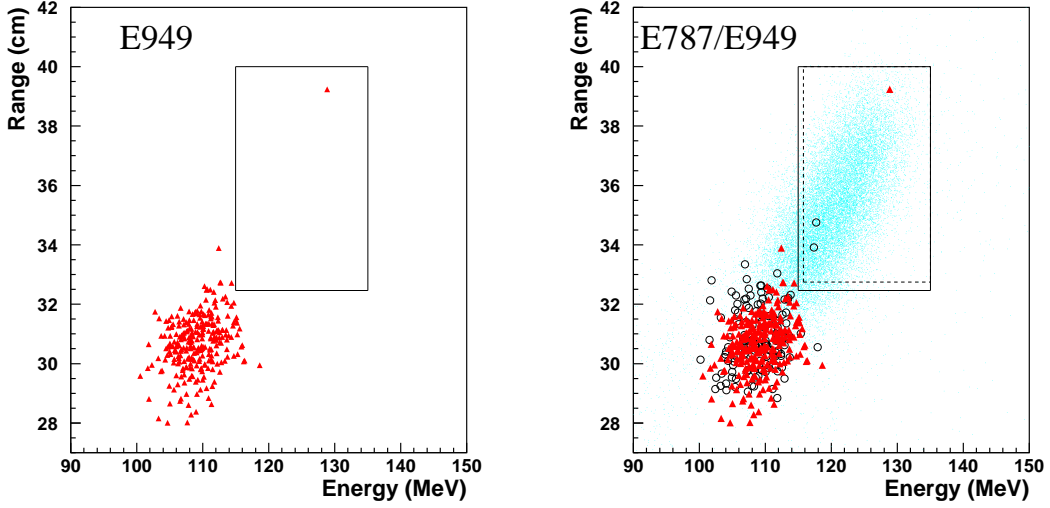


Figure 1: Energy vs range plots. **THIS IS A PLACEHOLDER ONLY.** Actual figures will show R vs E(or P) of E949 pnn2 candidates and R vs E(or P) of all candidates.

References

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